

1. Use factor theorem to determine whether $x + \sqrt{2}$ is a factor of $2\sqrt{2}x^2 + 5x + \sqrt{2}$.
2. Find the value of k if $(x - 3)$ is a factor of $k^2x^2 - kx - 2$.
3. Find the values of a and b so that the polynomial $x^3 - ax^2 - 13x + b$ has $x - 1$ and $x + 3$ as factors.
4. Without actual division, prove that $2x^4 - 6x^3 + 3x^2 + 3x - 2$ is exactly divisible by $x^2 - 3x + 2$.
5. What must be added to $x^3 - 3x^2 + 4x - 13$ to obtain a polynomial which is exactly divisible by $x - 3$?
6. What must be subtracted from $4x^3 + 16x^2 - x + 5$ to obtain a polynomial which is exactly divisible by $x + 5$?
7. If the polynomials $px^3 + 4x^2 + 3x - 4$ and $x^3 - 4x + p$ are divided by $x - 3$ then the remainder in each case is the same. Find the value of p .
8. If $x^3 + px^2 + qx + 6$ leaves remainder 3 when divided by $x - 3$ and 0 when divided by $x - 2$ Find the values of p and q .
9. If $2x^3 + ax^2 + bx - 6$ has $x - 1$ as a factor and leaves a remainder 2 when divided by $x - 2$, find the value of a and b .
10. Factorise $x^3 - 3x^2 - 10x + 24$ given that $x - 2$ is a factor.
11. Find the value of $a^3 + b^3 + c^3 - 3abc$, if $a + b + c = 14$ and $a^2 + b^2 + c^2 = 60$.
12. If $a + b + c = 0$, then prove that $\frac{a^2}{bc} + \frac{b^2}{ca} + \frac{c^2}{ab} = 3$
13. Factorise: $(2x - 3y)^3 + (3y - z)^3 + (z - 2x)^3$
14. Prove that: $a^3 - 8b^3 + 27c^3 + 18abc = 0$ when $a + 3c = 2b$
15. If $x + \frac{1}{x} = 5$, evaluate $x^4 + \frac{1}{x^4}$.