

QUESTION BANK

CLASS X

MATHEMATICS PRACTICE PAPER TOPIC

TRIGONOMETRY

- Evaluate:  $\sin 31^\circ \sec 59^\circ + \left(\frac{\tan 67^\circ}{\cot 23^\circ}\right)^2 + \sin^2 35^\circ - \cos^2 55^\circ$ .
- If  $\tan A + \sec A = a$ , show that  $\frac{a^2-1}{a^2+1} = \sin A$
- Prove that  $\frac{\sin \theta}{1-\cos \theta} + \frac{\tan \theta}{1+\cos \theta} = \sec \theta \operatorname{cosec} \theta + \cot \theta$
- Find the value of  $\cos 15^\circ$  using the formula  $\cos(A-B) = \cos A \cos B + \sin A \sin B$
- If  $\cot A + \frac{1}{\cot A} = 2$ , then prove that  $\cot^2 A + \frac{1}{\cot A \cdot \cot A} = 2$
- If  $\tan \theta = \frac{a}{b}$  Prove that  $\frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta} = \frac{b+a}{b-a}$
- If  $x \sin^3 \square + y \cos^3 \square = \sin \square \cos \square$  and  $x \sin \square = y \cos \square$  Prove that  $x^2 + y^2 = 1$
- If  $7 \operatorname{cosec} \square - 3 \cot \square = 7$  Prove that  $7 \cot \square - 3 \operatorname{cosec} \square = \pm 3$
- If  $\tan A = \frac{1}{2}$  and  $\tan B = \frac{1}{3}$  by using  $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$  10. Evaluate :  

$$\frac{\sin 15^\circ \cos 75^\circ + \cos 15^\circ \sin 75^\circ}{\tan 5^\circ \tan 30^\circ \tan 35^\circ \tan 55^\circ \tan 85^\circ}$$
- If  $\tan(A+B) = \sqrt{3}$  and  $\tan(A-B) = \frac{1}{\sqrt{3}}$ ;  $0 < A+B \leq 90$ ,  $A > B$  find A and B
- Find the value of  $\sec 50^\circ \sin 40^\circ + \cos 40^\circ \operatorname{cosec} 50^\circ$
- If  $\sin \square + \cos \square = \sqrt{2} \cos(90 - \square)$  determine  $\cot \square$
- Solve for  $\square$  :  $\sin^2 \theta = \frac{1}{2}$ ;  $0^\circ < \theta < 90^\circ$
- Prove that  $(\sqrt{3} + 1)(3 - \cot 30^\circ) = \tan^3 60^\circ - 2 \sin 60^\circ$
- If  $1 + \sin^2 \square = 3 \sin \square \cos \square$  then prove that  $\tan \square = 1$  or  $\frac{1}{2}$
- Determine for x :  $2 \operatorname{cosec}^2 30^\circ + x \sin^2 60^\circ - \frac{3}{4} \tan^2 30^\circ = 10$
- Prove that  $\frac{\sqrt{1+\sin \square}}{\sqrt{1-\sin \square}} + \frac{\sqrt{1-\sin \square}}{\sqrt{1+\sin \square}} = 2 \sec \square$
- Evaluate:-

$$(\cos^2 25^\circ + \cos^2 65^\circ) + \operatorname{cosec} \theta \sec (90^\circ - \theta) - \cot \theta \cdot \tan (90^\circ - \theta)$$

20. If  $\cos A = \frac{12}{13}$ , find the value of all other trigonometric ratios.

21. Prove that  $\sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = \sec\theta - \tan\theta$

22. Prove that :-  $\sin\theta(1 + \tan\theta) + \cos\theta(1 + \cot\theta) = \sec\theta + \operatorname{cosec}\theta$  .

23. Evaluate:-

$$(\sin^2 25^\circ + \sin^2 65^\circ) + \sqrt{3} (\tan 5^\circ \tan 15^\circ \tan 30^\circ \tan 75^\circ \tan 55^\circ)$$

24. Prove that  $\frac{1}{1+\sin\theta} + \frac{1}{1-\sin\theta} = 2 \sec^2\theta$

25. Prove that :-

$$(\operatorname{Cosec} A - \sin A)(\sec A - \cos A) = \frac{1}{\tan A + \cot A}$$

26. If  $\sin\theta = \frac{3}{5}$  Find the value of  $(\tan\theta = \sec\theta)^2$

27. If  $7 \sin^2\theta + 3 \cos^2\theta = 4$ , show that  $\tan\theta = \frac{1}{\sqrt{3}}$

28. Find the value of  $\tan 60^\circ$  geometrically.

29. Prove :  $\frac{\sec A + \tan A - 1}{\tan A - \sec A + 1} = \frac{1 + \sin A}{\cos A}$  .

30. Prove that:  $\frac{1 + \cos A}{\sin A} + \frac{\sin A}{1 + \cos A} = 2 \operatorname{cosec} A$

31. Prove that:  $\frac{1 + \sin A}{1 - \sin A} = (\sec A + \tan A)^2$

32. If A, B, C are interior angles of  $\Delta ABC$ , then show that:  $\cos\left(\frac{B+C}{2}\right) = \sin\frac{A}{2}$  .

33. Evaluate:  $\frac{\sin 39^\circ}{\cos 51^\circ} + 2 \tan 11^\circ \tan 31^\circ \tan 45^\circ \tan 59^\circ \tan 79^\circ - 3(\sin^2 21^\circ + \sin^2 69^\circ)$

34. If  $\tan(A+B) = 1$  and  $\sin(2A-B) = 1$  find A and B

35. If  $\operatorname{Cosec}\theta - \sin\theta = m$  and  $\sec\theta - \cos\theta = n$  prove that  $(m^2n)^{2/3} + (mn^2)^{2/3} = 1$

36. If  $a \cos^3\theta + 3a \cos\theta \sin^2\theta = m$  and  $a \sin^3\theta + 3a \cos^2\theta \sin\theta = n$  prove that  $(m+n)^{2/3} + (m-n)^{2/3} = 2a^{2/3}$

37. If  $2\cos\theta - \sin\theta = x$  and  $\cos\theta - 3\sin\theta = y$  prove that  $2x^2 + y^2 - 2xy = 5$  .